Model Residuals as Shields: A Bilevel Formulation to Defend Smart Grids from Poisoning Attacks

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***Abstract*—The advancement of interconnected smart grids brings both vast opportunities and heightened cybersecurity risks. Data-driven defense mechanisms, though devised as a shield against these threats, can fall prey to poisoning attacks. We delve into regression settings, underscoring the imperative to fortify defenses against a spectrum of poison ratios, notably those exceeding 0.5—a topic scarcely addressed in prior studies. Recognizing the susceptibilities of smart grids and their manipulable sensors, we exploit the very intent of poisoning attacks—compromising model accuracy—as our defense mechanism. Our proposed bilevel-optimization framework adeptly discerns between poisoned and authentic data based on model residuals, achieving impressive precision and recall. Once sanitized, this model is adaptable for varied applications. Comprehensive evaluations on different smart grid datasets, pitted against myriad poisoning schemes, validate our methodology's edge over existing methods. We also shed light on the implications of model misspecification stemming from temporal autocorrelation, a common feature in IoT and smart grid data.**

***Index Terms*—Adversarial machine learning, poisoning attack, kernel ridge regression, regression, IoT cybersecurity**

I. Introduction

Internet-of-things (IoT) and sensor technology transform power systems into smart grids, integrating renewable energy and optimizing power consumption [1]. These grids function as interconnected systems that depend heavily on communication channels for data flow among generators, sensors, and controllers [2]. However, the interconnectedness exposes them to potential threats that compromise their security, resulting in extensive damages [3]. Robustness in these infrastructures is a priority.

A challenge in IoT and smart grid security is the integrity of data acquired from sensors. Sensors serve as primary data sources and are prone to adversarial attacks or noise interference. Therefore, machine learning (ML) detectors are often deployed to verify incoming data. Yet, there's a notable weak point in data-driven detectors: they can fall victim to *poisoning attacks*, where the training data collected from sensors are corrupted by environmental noise or intentional adversaries [4]. Defense measures against outliers or poisoning attacks in the training data encompass: 1) Input space detection, which leans on robust statistical measures, although often neglecting higher-order nuances [5]. 2) Latent space techniques, specifically designed for neural networks [6]. 3) Prediction signatures, utilizing tools like saliency maps but largely confined to classification tasks such as image recognition [7]. 4) Other methods, including majority voting and differential privacy, but generally assuming a small poisoning ratio [8]. A review of existing literature highlights two primary challenges.

Poisoning attacks in regression settings. While much research centers on classification settings [4], [9], the criticality of regression in smart grids—for tasks like demand prediction and state estimation—presents unique challenges. Unlike classification that targets decision boundaries, poisoning in regression discreetly adjusts predictions, affecting the model's gradient. Such nuanced alterations not only challenge defenses but also escalate risks, since minor deviations in smart grids can result in significant inefficiencies or failures.

Defense against high poison ratios. Diving deeper, an often-overlooked aspect is the criticality of the poison ratio. The majority of studies limit the effectiveness of their methods when the poison ratio is below 0.05 [5] or 0.2 [10]. Yet, our findings indicate a deterioration in performance as this ratio nears 0.5 (refer to Table II). It's acknowledged that M-estimators [11] have an upper limit breakdown point of 0.5 [12]. Although [13] explores high poison ratios in linear regression, it presupposes knowledge of the exact poison ratio and relies on specific distributional assumptions—often unrealistic in practice. Given the diverse data sources in smart grids, from users to smart meters and IoT devices, the potential for external tampering grows. *A high poison ratio (potentially beyond 0.5) prompts a reexamination of current methodologies.* In an environment where the signal masquerades as noise (and vice versa), reliance on conventional techniques becomes questionable. If left unchecked, models derived from such tainted datasets risk significant inaccuracies, potentially jeopardizing grid operations and efficacy.

Contributions & key insights: At their core, poisoning attacks seek to disrupt model accuracy, drastically skewing predictions. This skewing, paradoxically, lights the way to counter these attacks. Generally, a model aligned with normal data will present variances consistent with typical statistical behaviors. However, a poisoned dataset disrupts this behavior, serving as a red flag. Instead of fixating on input features, which can naturally vary, our focus is on the *model's residuals*. Our observations underscore a compelling dichotomy: models optimized for normal data struggle with poisoned datasets and vice versa, drawing a clear line between them.

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Building upon this insight, our methodology tentatively divides data into hypothetical 'normal' and 'poisoned' categories. By training a model to one subset and measuring its error on the other, an iterative refinement of this categorization is possible. This approach is especially adept at navigating high poison ratios in regression contexts. Technically, we employ a bilevel optimization strategy: the inner level focuses on "model training" (e.g., kernel ridge regression), while the outer level seeks to optimize the partition to maximize error differences. We also consider cases where poison ratios approach or exceed 0.5, using the list-decodable setting [13] for evaluation. Our evaluation across diverse smart grid datasets, encompassing various poison ratios and attack methods, indicates that our approach consistently outperforms existing methodologies. Notably, we sidestep the need of predetermined poison ratios, aligning closer with realistic conditions. Compared to state-of-the-art methods such as [10], our method distinguishes between normal and poisoned data with high precision and recall metrics. Beyond data partitioning, the resultant nonlinear model, characterized by its low regression error, is suitable for practical applications. If further model refinement is necessary, the isolated normal dataset provides a reliable foundation.

The remainder of this paper is organized as follows: Sec.II reviews relevant literature on attacks in smart grid systems and the broader realm of robust machine learning. Our proposed methodology is detailed in Sec.III. Experimental setups and findings are shown in Sec.IV. The paper concludes in Sec. V.

II. Related Work

Security challenges in IoT and smart grids have prompted the development of data-driven detectors against various threats. Random forest and neural networks have been explored for jamming attacks that disrupt wireless networks [14]. For electricity theft, wherein customers alter meter readings to reduce bills, studies employ outlier detection [15] and deep learning methods [16]. The data-centric nature of these detectors makes them susceptible to poisoning attacks [17]. Neural networks, although promising, might not always be the preferred choice. In contexts where computational resources are limited or where model interpretability is crucial, the tilt is towards more transparent models such as linear regression, as seen in distributed energy management systems [18] and smart home power monitoring [19].

Robust linear regression against poisoning attacks has recently garnered attention, yet many works cap the poison ratio at a mere 0.05 [5] or 0.2 [10] in their evaluations. Given the open nature of smart grids and potential sensor tampering [20], the training set can exhibit higher poison ratios. For example, sensor tampering was evaluated with a poison ratio of up to 0.7 in [21]. When the majority of a dataset is poisoned, the list-decodable setting [13] produces multiple functions, one aligning with the ground truth. In our study, we utilize the list-decodable setting for poison ratios of 0.5 and above. Moreover, while the bulk of existing literature assumes data drawn independently from an inherent distribution, we explore model misspecification stemming from autocorrelation in time series data—a prevalent scenario where data originate from sensor measurements.

III. Methodology

Let the dataset be denoted as $\mathcal{D} = \{(x_i, y_i)_{i\in[n]}\}$, where $[n]$ is shorthand for the set $\{1, ..., \}$. The features are represented by $X = \{x_i\}_{i=1}^n \in \mathbb{R}^{n\times d}$ and labels by $Y = \{y_i\}_{i=1}^n \in \mathbb{R}^n$. We consider $\mathcal{H}$ as a Reproducing Kernel Hilbert Space (RKHS) with kernel, $k : \mathbb{R}^d \times \mathbb{R}^d \to \mathbb{R}$, such as the polynomial or Radial Basis Function (RBF) kernel. The objective is to identify a function $f : \mathbb{R}^d \to \mathbb{R}$ within $\mathcal{H}$ that yields minimal prediction error for a given feature x amidst the presence of poisons in $\mathcal{D}$.

To crystallize our idea, we define $\mathcal{N}(w) = \{i : w_i = 1\}$ as the index set of hypothetical normal data, with each data point i having a binary weight $w_i \in \{0, 1\}$. Conversely, $\mathcal{P}(w) = \mathcal{N}(1 - w) = \{i : w_i = 0\}$ denotes the index set for the hypothetical poisoned data, being the complement to $\mathcal{N}(w)$. While the hypothesis $w \in \{0, 1\}^n$ delineates the membership sets, the tags of 'normal' or 'poison' merely represent dual data facets; their true nature could be swapped. Within a list-decodable setting, we can train a model using either $\mathcal{N}(w)$ or $\mathcal{P}(w)$ data. Success is declared if one model proves to be accurate. Typically, discerning between the poisoned and normal datasets becomes straightforward upon examination. Now, if we define $\mathcal{L}(f; \mathcal{D}, w) = \frac{1}{\|w\|_1} \sum_{i\in\mathcal{N}(w)} \ell\big(f(x_i), y_i\big)$ as the average error of model f evaluated on hypothetical data defined by w, then $f_w^* = \arg\min_{f\in\mathcal{H}} \mathcal{L}(f; \mathcal{D}, w)$ is the model trained on this hypothetical normal set. We posit that by identifying a hypothesis w, such that the model f_w^*, when trained on the hypothetical normal set, maximizes the error on the hypothetical poisoned set $\mathcal{P}(w)$, it becomes feasible to separate the poisoned data from normal data, resulting in the selection of a dependable model from either f_w^* or f_{1-w}^*.

Building upon the preceding theoretical discussion, we present a bilevel optimization framework as follows:

$$\begin{aligned} \max_{\{w_i\}_{i=1}^n} \quad & \frac{1}{\|1 - w\|_1} \sum_{i\in\mathcal{P}(w)} \big(y_i - f_w^*(x_i)\big)^2 \\ \text{s.t.} \quad & f_w^* = \arg\min_{f\in\mathcal{H}} \sum_{i\in\mathcal{N}(w)} \big(y_i - f(x_i)\big)^2 + \lambda\|f\|_{\mathcal{H}}^2 \\ & w_i \in \{0, 1\}, \quad \forall i \in [n] \end{aligned} \tag{1}$$

Within this framework, the inner level of (1) deduces the best f_w^* from hypothetical normal data, whereas the outer level seeks a w such that f_w^* maximizes the average residuals for the hypothetical poisoned data. Given our focus on regression, we employ squared loss for $\ell(\cdot)$. Moreover, the norm $\|\cdot\|_{\mathcal{H}}$ linked to $\mathcal{H}$, weighted by hyperparameter $\lambda \in \mathbb{R}_+$, serves to regularize smoothness in f. This stems from the rationale that genuine functions tend towards smoothness, in contrast to their aberrant counterparts that may show pronounced fluctuations.

Continuous relaxation of the hypothesis vector. The formulation given by (1) is essentially a mixed-integer quadratic problem, which is NP-hard in general. In pursuit of computational tractability, we relax the discrete variable set $\{w_i\}_{i=1}^n$ to be real-valued within the interval $[0, 1]$. To provide even more flexibility, we further extend their domain to $\mathbb{R}$ and subsequently apply the Sigmoid function: $s(w_i) = (1 + e^{-Tw_i})^{-1}$, where $T \in \mathbb{R}_+$ acts as a temperature parameter, modulating

the smoothness of $s(\cdot)$. Accordingly, the related formulation can be written as:

$$\begin{aligned} \max_{\{w_i\}_{i=1}^n} \quad & \frac{1}{\sum_{i=1}^n \big(1-s(w_i)\big)} \sum_{i=1}^n \big(1-s(w_i)\big)\big(y_i - f_w^*(x_i)\big)^2 \\ s.t. \quad & f_w^* = \arg\min_{f\in\mathcal{H}} \sum_{i=1}^n s(w_i)\big(y_i - f(x_i)\big)^2 + \lambda\|f\|_{\mathcal{H}}^2 \\ & w_i \in \mathbb{R}, \quad \forall i \in [n] \end{aligned} \tag{2}$$

Reduction to single-level optimization. Despite the continuous relaxation above, the computational complexity of a bilevel optimization remains. Nevertheless, by invoking the representer theorem [22], we can derive the unique optimal solution for the inner level. Specifically, this solution can be expressed as: $f(x) = \sum_{i=1}^n \alpha_i k(x, x_i)$, where $\alpha = \{\alpha_i\}_{i=1}^n \in \mathbb{R}^n$. Substituting this expression into the inner level of (2) to determine the optimal α^* yields: $\alpha^* = \big(S(w)K + \lambda I\big)^{-1} S(w)Y$, where $S(w)$ is a diagonal matrix with $S(w)_{i,i} = s(w_i)$. Additionally, $K \in \mathbb{R}^{n\times n}$ is the kernel matrix defined such that $K_{i,j} = k(x_i, x_j)$, and I is the identity matrix.

Consequently, our bilevel optimization problem can be reduced to a single-level optimization. By substituting $f_w^* = \sum_{i=1}^n \alpha_i^* k(x, x_i)$ into the outer optimization, we can express the problem in a vectorized form as:

$$\max_{w\in\mathbb{R}^n} \quad H(w) \coloneqq \frac{1}{\operatorname{Tr}\big(I - S(w)\big)} \Big(\big(I - S(w)\big)^{\frac{1}{2}} (Y - \Lambda) \Big)^2, \tag{3}$$

where $\Lambda \coloneqq K\big(S(w)K + \lambda I\big)^{-1} S(w)Y$ and $\operatorname{Tr}(\cdot)$ denotes the trace operation.

The problem posed by (3) is a non-concave maximization problem, lacking discernible structure. Consequently, we employ gradient ascent to solve it. The gradient of $H(w)$ with respect to w_i is analytically derived as:

$$\begin{aligned} \frac{\partial H(w)}{\partial w_i} \quad = & \frac{s'(w_i)}{\Big(\operatorname{Tr}\big(I - S(w)\big)\Big)^2} \Big(\big(I - S(w)\big)^{\frac{1}{2}} (Y - \Lambda) \Big)^2 \\ & + \frac{1}{\operatorname{Tr}\big(I - S(w)\big)} \Bigg(s'(w_i)(-y_i^2 + 2\Lambda_i y_i - \Lambda_i^2) \\ & + \Big(2(\Lambda - Y)^\top \big(I - S(w)\big) \Big) \frac{\partial \Lambda}{\partial w_i} \Bigg), \end{aligned} \tag{4}$$

where $\frac{\partial \Lambda}{\partial w_i} = K\big(S(w)K + \lambda I\big)^{-1} e_i s'(w_i) \big(e_i^\top (Y - \Lambda)\big)$, e_i is the canonical unit vector with the i-th entry being 1 and others being 0, and $s'(w_i)$ is the derivative of $s(w_i)$. A detailed derivation is in App. B.

Scalability via Random Fourier Features (RFF). To evaluate (4), we must compute both Λ and $\frac{\partial \Lambda}{\partial w_i}$, which entails the inversion of an $n\times n$ matrix $\big(S(w)K + \lambda I\big)^{-1}$. The complexity of this inversion increases with the dataset's size, presenting a computational bottleneck intrinsic to kernel methods. To address this, we utilize the RFF approximation [23], which estimates shift-invariant kernels, encompassing the widely-used RBF kernel defined by $k(x_i, x_j) = \exp(-\gamma\|x_i - x_j\|^2)$, where $\|\cdot\|$ denotes the Euclidean distance.

In the RFF approach, the Fourier transform of the kernel is sampled randomly p times, and this sampling transforms the raw data x_i into a p-dimensional space. E.g., $z(x_i) = \sqrt{\frac{2}{p}} \big[\cos(\omega_1^\top x_i + b_1), \cdots, \cos(\omega_p^\top x_i + b_p)\big]^\top$, where $\omega_i \sim q(\omega), b_i \sim \text{Uniform}(0, 2\pi)$, and $q(\omega)$ is the Fourier transform of the kernel. Leveraging Bochner's Theorem and defining Z as the $n \times p$ matrix with its i-th row given by $z(x_i)^\top$, we can approximate K by $ZZ^\top$ (refer to [23] for a comprehensive exposition). With RFF approximation and the Woodbury identity, we can sidestep the necessity of inverting an $n \times n$ matrix. To elucidate:

$$\begin{aligned} \Lambda \quad & = K(S(w)K + \lambda I)^{-1} S(w)Y \\ & \approx ZZ^\top (S(w)ZZ^\top + \lambda I)^{-1} S(w)Y \\ & = Z(Z^\top S(w)Z + \lambda I)^{-1} Z^\top S(w)Y \coloneqq Z\theta. \end{aligned} \tag{5}$$

This approach grants us the flexibility to manage computational complexity directly since the operation revolves around inverting a $p \times p$ matrix. A larger p enhances approximation accuracy but concurrently increases computational cost.

Algorithm 1 Gradient Ascent

Inputs: data X, Y, regularization hyperparameter λ, temperture parameter T, number of samples for RFF approximation p, kernel function k, number of iterations for gradient ascent t, learning rate β

Output: $\mathcal{N}(\bar{w}), \mathcal{P}(\bar{w})$, $f_{\bar{w}}^*, f_{1-\bar{w}}^*$

Calculate the Fourier transform q of k
Draw p i.i.d. samples $\omega_1, \ldots, \omega_p$ from q and $b_1, \ldots, b_p$ from Uniform$(0, 2\pi)$
Construct Z, whose i-th row is $z(x_i) = \sqrt{\frac{2}{p}}[cos(\omega_1^\top x_i + b_1), \cdots, cos(\omega_p^\top x_i + b_p)]$
Initialize $w^{(1)} = 0$
for $j = 1, 2, \ldots, t$ **do**
  $w^{(j+1)} = w^{(j)} + \beta \nabla_w H(w^{(j)})$
  // $\nabla_w H(w^{(j)})$ is calculated according to (4)
end for
$\{\bar{w}_i\}_{i=1}^n \leftarrow$ Round $\{s(w_i)\}_{i=1}^n$ to the nearest integer
$\mathcal{N}(\bar{w}) = \{i : \bar{w} = 1\}, \mathcal{P}(\bar{w}) = \{i : \bar{w} = 0\}$
$f_{\bar{w}}^*(x) = z(x)^\top (Z^\top diag(\bar{w}) Z + \lambda I)^{-1} Z^\top diag(\bar{w}) Y$
$f_{1-\bar{w}}^*(x) = z(x)^\top (Z^\top diag(1-\bar{w}) Z + \lambda I)^{-1} Z^\top diag(1-\bar{w}) Y$
return $\mathcal{N}(\bar{w}), \mathcal{P}(\bar{w}), f_{\bar{w}}^*, f_{1-\bar{w}}^*$

Algorithm. The outlined procedure is detailed in Alg. 1. Upon convergence of the gradient ascent, $s(w_i)$ serves as an indicator of the contribution of the i-th data point towards the learning of f_w^*. Specifically, when $s(w_i)$ approaches 1, it implies that the data point (x_i, y_i) has notably influenced the learning of f_w^*. Given that the choice to use a data point for f_w^* is inherently binary, we round $s(w_i)$ to the nearest integer, either 0 or 1, and denote the result as $\bar{w}_i$. This step enables us to discern and segregate the learned normal dataset, $\mathcal{N}(\bar{w})$, from the complementary set of anomalous or poisoned data, $\mathcal{P}(\bar{w})$.

IV. Experiments

Datasets. The Stability dataset [24] examines a decentralized four-node electrical system's local stability, focusing on 11 features such as participant reaction time and nominal power consumption. The goal is to predict the maximal real

part of a characteristic equation root, where positive indicates instability and negative denotes stability. The DERMS dataset [18] revolves around a smart grid's Distributed Energy Resource Management System (DERMS). It logs measurements sent to and actions from the DERMS controller, covering features including real and reactive powers, and each node's maximum inverter generation limit. Predictions from this dataset assist in detecting deviations in control actions, signaling potential intrusions. The House dataset [25] describes a low-energy home's electricity usage through 28 features like kitchen humidity and local weather data. It forecasts the household's total appliance energy consumption, aiding in anomaly detection or demand management. Lastly, the CCPP dataset [26] delves into a Combined Cycle Power Plant, capturing 4 features such as ambient temperature/humidity and exhaust vacuum. The objective is to predict the plant's net hourly energy output.

Poisoning Attacks. We outline the data poisoning attacks used in our experiments. Given a normal dataset $\mathcal{D}_n$, their goal is to construct the resultant dataset $\mathcal{D} = (\mathcal{D}_n \setminus \mathcal{D}_t) \cup \mathcal{D}_p, \mathcal{D}_t \subset \mathcal{D}_n$, with $\mathcal{D}_t$ representing tampered data from $\mathcal{D}_n$ and $\mathcal{D}_p$ as the injected poisons. The *poison ratio* is given by $\frac{|\mathcal{D}_p|}{|\mathcal{D}|}$.

In the Optimization-Based Injection [27], a bilevel optimization framework crafts $\mathcal{D}_p$. The attacker, knowing dataset $\mathcal{D}'$ (similar to $\mathcal{D}_n$) and loss function $\ell(\cdot)$, maximizes the average loss on a validation set using an optimal model from the inner level. This model represents the impact of injecting $\mathcal{D}_p$ into $\mathcal{D}_n$. In tests, we set $\mathcal{D}' = \mathcal{D}_n$, implying full attacker knowledge. The Flip method [10] also uses a similar dataset, but without requiring access to the loss function. Poisons are crafted based on a feasibility domain of the labels to avert suspicion, and each poison corresponds to data points in $\mathcal{D}'$. Like before, $\mathcal{D}' = \mathcal{D}_n$ in our tests, which allows us to consider a poison ratio of 0.5. In the Additive Attack [21], labels in $\mathcal{D}_n$ are modified by adding a fixed value, $\delta_a = 2$ in our tests. This misleads the model to predict higher values. Lastly, in Noise Corruption, labels in $\mathcal{D}_n$ are altered using values from a distribution, specifically $\delta_n \sim N(0, 0.2)$ in our tests, reflecting data acquisition noise.

The first two attacks maintain $\mathcal{D}_n$ while introducing extra poisons ($\mathcal{D}_t = \{\phi\}$), which require database access. However, such attacks are not always possible, such as the case when the number of data entries is pre-set. On the other hand, the last two attacks directly change the labels in $\mathcal{D}_n$ ($\mathcal{D}_t \neq \{\phi\}$), which can happen during data acquisition.

Baseline Defenses. iTRIM [10] iteratively refines the function f by focusing on data subsets with the smallest residuals across different poison ratios. Huber loss [11] combines the sum of squares loss and sum of absolute values loss. Lastly, Sever [5], assuming the true poison ratio, filters out data points with notably strong projected gradients on the leading singular vector of the gradient matrix.

Setup. The proposed method is implemented in Python while the baseline defenses are from the sklearn package [28] or the authors [5], [10] respectively. For each dataset, we randomly select $8,000$ to $10,000$ data points as $\mathcal{D}_n$ and use the rest as the test set. Both the features and labels are scaled to the range $[0, 1]$. The regularization hyperparameter λ is set to 0.01, the temperature T to 0.5, the number of draws for RFF p to 200, the number of iterations to 3500, the learning rate β to 0.01, and the RBF kernel as k.

Evaluation Metrics. To evaluate the partition of $\mathcal{D}$ into poisons and normal data, we define poisons as positives, normal data as negatives, and calculate the precision and recall. Denote true positives, false positives, true negatives, and false negatives as TP, FP, TN, FN, respectively. Precision and recall can be calculated as follows. precision $= \frac{\text{TP}}{\text{TP+FP}}$ and recall $= \frac{\text{TP}}{\text{TP+FN}}$. Moreover, we evaluate the model learned from the partitioned normal data on the test set using mean squared error (MSE). In the following, we refer to MSE as the test MSE unless stated otherwise.

A. Poison Ratio Smaller Than 0.5

In this section, we vary the poison ratio from 0 to 0.4.

Does the proposed method partition data more effectively? High precision signifies a reduced chance of erroneously classifying normal data as poisoned, while high recall indicates a reduced chance of mistakenly identifying poisoned data as normal. Both these measures are indicative of effective data partitioning. In Table I, we juxtapose the precision and recall of our approach with that of iTRIM. For the additive attack, our method consistently delivers nearly 100% precision and recall across various datasets and poison ratios. We also observe substantially higher precision and recall for Flip and Optimization-based attacks using our approach. For noise corruption scenarios, the precision and recall metrics for both methods drop in comparison to other attack types. This decline can be attributed to the fact that the noise, δ_n, is sampled from a distribution $N(0, 0.2)$. Consequently, if a sampled noise has a small magnitude, it does not significantly impact the poisoning effect on f.

Does a better partition lead to a better model? We show the test MSEs of the model learned from the oracle and baseline methods in Fig. 1. The oracle is the data partition with 100% precision and recall. In the following, we discuss the case when the poison ratio is above and at zero separately.

At poison ratios above zero, our method has the smallest MSEs compared with the baselines except for under Flip and additive attack on DERMS. The reason is that DERMS is heavily autocorrelated (See App. A for the autocorrelation profile of each dataset.). This model misspecification brings about the fact that higher precision and recall don't necessarily lead to lower MSE of the resultant model. iTRIM achieves lower MSEs by sacrificing precisions as shown in Table I. By using kernel ridge regression, we assume the data follow $y = z(x)^\top \theta + \epsilon$, where ϵ denotes the error that includes model misspecification error and i.i.d. noise. According to the Gauss-Markov theorem [29], linear regression is only the best linear unbiased estimator (BLUE) when ϵ is uncorrelated; otherwise, it leads to inflated MSEs. Therefore, by removing normal data with high model misspecification errors, iTRIM achieves lower MSEs. When the sifted normal data is used for fitting sophisticated downstream models, a lower precision may lead to degraded performance. Note that for a fair comparison, we leave the poison ratio parameter in Sever [5] as default in its

TABLE I: Precision / Recall (%) at poison ratios smaller than 0.5

	Stability								DERMS							
	Flip		Opt		Add		Noise		Flip		Opt		Add		Noise	
ratio	Ours	iTRIM	Ours	iTRIM	Ours	iTRIM	Ours	iTRIM	Ours	iTRIM	Ours	iTRIM	Ours	iTRIM	Ours	iTRIM
0.1	**100**/**100**	93.2/**100**	**99.9**/**100**	93.2/**100**	**99.9**/**100**	93.2/**100**	35.2/**67.8**	**83.8**/32.3	**85.5**/**96.7**	63.3/96.6	**70.4**/**95.6**	62.6/**95.6**	**100**/**100**	65.5/**100**	14.1/6.4	**34.3**/**31.3**
0.2	**100**/**100**	96.9/**100**	**100**/**100**	96.9/**100**	**100**/**100**	96.9/**100**	60.4/**60.4**	**94.0**/26.6	**98.0**/**97.9**	80.8/**97.9**	**92.0**/**96.0**	78.9/95.7	**100**/**100**	82.5/**100**	24.8/5.7	**52.3**/**28.0**
0.3	**100**/**100**	98.2/**100**	**100**/**100**	98.2/**100**	**100**/**100**	98.2/**100**	78.2/**54.7**	**97.3**/24.0	**96.4**/**98.1**	88.3/**98.1**	**95.3**/90.6	88.2/**95.4**	**100**/99.9	87.7/**100**	34.8/5.5	**64.1**/**26.3**
0.4	**100**/**100**	10.0/7.4	**100**/99.9	98.8/**100**	**100**/**100**	98.8/**100**	87.3/**49.7**	**98.6**/22.4	97.8/**97.8**	**99.6**/18.5	**97.5**/94.0	92.7/**95.4**	**100**/**100**	92.6/**100**	45.9/5.5	**73.8**/**25.5**
	House								CCPP							
	Flip		Opt		Add		Noise		Flip		Opt		Add		Noise	
ratio	Ours	iTRIM	Ours	iTRIM	Ours	iTRIM	Ours	iTRIM	Ours	iTRIM	Ours	iTRIM	Ours	iTRIM	Ours	iTRIM
0.1	**98.7**/**99.9**	72.4/**99.9**	**90.9**/**98.8**	80.3/**98.7**	**99.9**/**100**	81.4/**100**	42.4/1.4	**46.7**/**26.4**	**99.1**/**100**	93.2/**100**	**98.0**/**100**	93.2/**100**	**100**/**100**	93.2/**100**	90.9/**33.3**	**93.2**/18.4
0.2	**99.2**/**100**	91.4/**100**	**98.0**/**99.2**	90.6/**99.2**	**100**/**100**	91.4/**100**	65.5/1.0	**67.0**/**24.9**	**99.8**/**100**	96.9/**100**	**99.7**/99.9	96.9/**100**	**100**/**100**	96.9/**100**	97.0/25.2	**97.1**/**27.5**
0.3	**99.6**/**100**	95.2/**100**	**99.8**/**99.2**	94.4/**99.2**	**100**/**100**	95.2/**100**	70.4/0.7	**76.2**/**23.1**	**99.9**/99.9	98.2/**100**	**99.8**/**100**	98.1/**100**	**100**/**100**	98.2/**100**	93.2/**53.1**	**98.2**/24.3
0.4	99.7/**99.1**	**99.8**/89.5	**100**/**99.2**	96.3/**99.2**	**100**/**100**	97.1/**100**	80.8/0.5	**84.2**/**22.6**	**100**/**99.9**	99.2/84.9	**99.9**/97.7	**99.9**/**99.3**	**100**/**100**	98.8/**100**	97.8/**43.9**	**98.7**/22.5

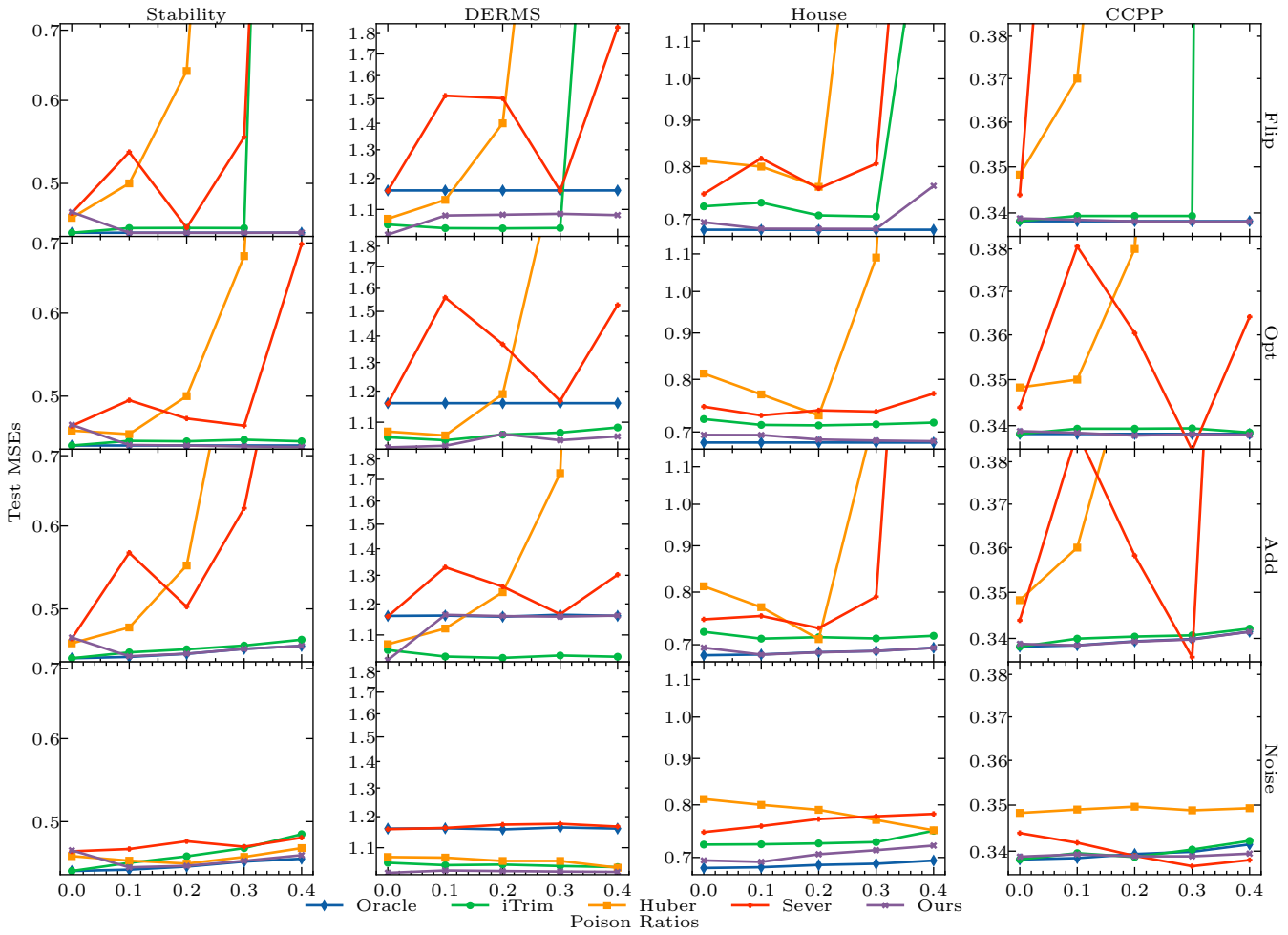

Fig. 1: **Test MSEs at poison ratios smaller than 0.5.** A partition with higher precision and recall leads to lower test MSE if little or no model misspecification exists. Lower test MSEs by iTRIM on DERMS are achieved by sacrificing precision because of model misspecification.

original implementation, which is 0.3. Hence, a drop in MSE is observed at 0.3 in several cases.

At a poison ratio of 0, corresponding to scenarios where no poisoning attack has occurred, the FPs and the associated MSEs are detailed in Table III. Huber is omitted from this discussion as it doesn't have the capability to filter out poisons. Without model misspecification, a lower FP count typically results in reduced MSEs. This relationship is evident in the cases of Stability and CCPP, where iTRIM reports 0 FP. However, in scenarios exhibiting significant autocorrelation, such as DERMS, having non-zero FPs can yield even lower MSEs than the oracle. This behavior sharply contrasts with the instances where DERMS registers a high precision but elevated MSE when the poison ratio exceeds 0. One potential reason for this observed behavior is that the outer level of equation (2) can result in a 'divide-by-zero' scenario if $w_i = 1$ for all $i \in [n]$. Consequently, at a poison ratio of 0, our methodology may incline towards omitting normal data points that exhibit pronounced model misspecification errors. This tendency, in turn, results in non-zero FPs but minimized MSEs.

B. *Poison Ratio at 0.5*

Is our method directly applicable to the list-decodable setting? When the poison ratio is exactly at 0.5, an inductive bias is necessary because there are an equal number of poisons and normal data. Our insight is that effective poisons are

TABLE II: Test MSEs at 0.5 poison ratio

	Stability							DERMS							House							CCPP						
	$\lambda = 0.01$				λ	Ours	Oracle	$\lambda = 0.01$				λ	Ours	Oracle	$\lambda = 0.01$				λ	Ours	Oracle	$\lambda = 0.01$				λ	Ours	Oracle
	iTRIM	Huber	Sever	Ours			MSE	iTRIM	Huber	Sever	Ours			MSE	iTRIM	Huber	Sever	Ours			MSE	iTRIM	Huber	Sever	Ours			MSE
Flip	28.48	9.39	23.50	3.16	10	**0.79**	0.45	51.39	18.20	65.89	25.01	50	**1.44**	1.16	29.35	21.35	58.46	8.78	100	**0.69**	0.68	32.31	12.10	29.45	0.56	50	**0.34**	0.34
Opt	27.41	10.44	23.33	1.83	0.1	**1.54**	0.45	52.17	18.92	62.74	2.39	100	**1.62**	1.16	47.97	21.41	44.46	22.51	0.1	**1.32**	0.68	43.93	12.74	37.66	0.50	0.1	**0.43**	0.34
Add	148.2	102.9	0.49	127.2	100	**0.47**	0.46	251.0	99.07	158.0	7.89	100	**1.16**	1.15	208.3	103.0	179.3	139.0	100	**0.69**	0.69	330.1	100.8	171.9	56.6	100	**0.34**	0.34
Noise	0.50	**0.47**	180	0.50	0.1	**0.47**	0.46	**1.04**	1.05	1.16	1.06	0.1	**1.04**	1.15	0.75	0.74	0.79	0.76	0.1	**0.73**	0.69	**0.34**	0.35	**0.34**	**0.34**	0.1	**0.34**	0.34

TABLE III: False positives and test MSEs of each method at 0 poison ratio

	iTRIM		Sever		Ours		Oracle	Training Set
	FP	MSE	FP	MSE	FP	MSE	MSE	Size
Stability	0	**0.449**	6072	0.468	253	0.470	**0.449**	8000
DERMS	652	1.055	6680	1.159	379	**1.025**	1.160	8800
House	377	0.723	7442	0.747	101	0.695	**0.681**	9800
CCPP	0	**0.338**	6831	0.344	31	0.339	**0.338**	9000

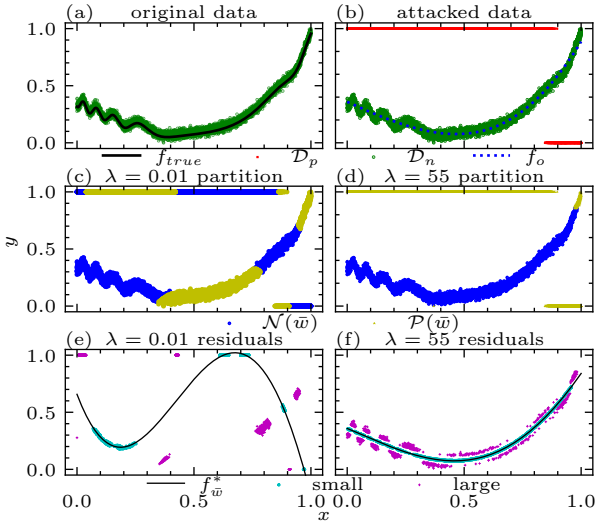

Fig. 2: **Visualization of synthetic data to illustrate the importance of inductive bias at 0.5 poison ratio.** When λ is increased from 0.01 to 55 to encourage smoothness, the partition becomes more ideal and the resultant model captures the true function better.

inevitably far from the normal data. Therefore, smoothness should be encouraged to prevent learning from portions of poisons and normal data.

We visualize the importance of inductive bias with a 1-dimensional synthetic dataset generated by drawing $10,000$ random samples in the range $x \in [-3, 2]$ from the noisy function $y = x^2 + sin(x^3) + exp(x + 1) - 2 + \xi$, where $\xi \sim N(0, 0.5)$. Both x and y are then scaled to $[0, 1]$. Among the $10,000$ data points, 8000 are used as $\mathcal{D}_n$ and the rest as the test set. $\mathcal{D}_n$ and the true function f_{true} are visualized in Fig. 2(a). Next, Flip creates $\mathcal{D}_p$ of size 8000, resulting in a 0.5 poison ratio in Fig. 2(b). We also show the oracle model f_o with $\lambda = 0.01$, whose test MSE is 0.085.

Fig. 2(c) visualizes $\mathcal{N}(\bar{w})$ and $\mathcal{P}(\bar{w})$ that our proposed method produces when $\lambda = 0.01$. An ideal partition in the list-decodable setting is either of the following cases: (i) $w_i \in \mathcal{N}(\bar{w})$ iff $w_i \in (\mathcal{D}_n \backslash \mathcal{D}_t)$, or (ii) $w_i \in \mathcal{P}(\bar{w})$ iff $w_i \in (\mathcal{D}_n \backslash \mathcal{D}_t)$. Nevertheless, in Fig. 2(c), both the poisons and the normal data are divided into sections by the partition. We further sample along the x axis and plot $f^*_{\bar{w}}(z(x))$ in Fig. 2(e), along with 1000 data points in $\mathcal{N}(\bar{w})$ with the largest and smallest residuals respectively. As illustrated, $f^*_{\bar{w}}$ with $\lambda = 0.01$ is a lot more wiggly than f_{true} because a highly wiggly function at 0.5 poison ratio that oscillates between poisons and normal data maximizes the outer objective function in (2). The test MSE in this case is 27.79, which is highly influenced by the poisons. Next, we increase λ to encourage a smooth $f^*_{\bar{w}}$. In Fig. 2(d), we set $\lambda = 55$ on line 6 in Alg. 1 to produce a more ideal partition. Subsequently, $f^*_{\bar{w}}$ is learned from $\mathcal{N}(\bar{w})$, setting $\lambda = 0.01$ on line 10 in Alg. 1 to compare with the test MSE from f_o. The test MSE is greatly reduced from 27.79 to 0.093 and the resultant $f^*_{\bar{w}}$ captures the true function much better as shown in Fig. 2(f).

Does the insight transfer to high-dimensional data? We attack the datasets at 0.5 poison ratio and compare the test MSEs of different defense methods. First, λ is set to 0.01 and the corresponding MSEs are presented in Table II. To discern which of $f^*_{\bar{w}}$ and $f^*_{1-\bar{w}}$ learns the normal data, a small set of 10 normal data points is partitioned from $\mathcal{D}_n$ to form a validation set. We only include the test MSE of $f^*_{\bar{w}}$ or $f^*_{1-\bar{w}}$, whichever has the smaller validation MSE. The results show that without an inductive bias, at $\lambda = 0.01$, all attacks increase the MSEs by a large margin, with one exception being noise corruption. The reason is similar to as mentioned in Sec. IV-A. Some δ_n may have small magnitudes, resulting in ineffective poisons.

Then, inductive bias is introduced by increasing λ on line 6 in Alg. 1. Specifically, we choose λ among $\{0.1, 10, 50, 100\}$ and select the one that has the lowest validation MSE at $\lambda = 0.01$. Note that λ on line 10 remains 0.01. As Table II shows, our test MSEs decrease to a more tolerable level for all cases. Results from other methods under different λ's are omitted because they either are insensitive to λ or produce unsatisfactory results compared with ours. The reason iTRIM yields unsatisfactory performance is that it initializes by learning f on the entire $\mathcal{D}$. This results in large residuals on both poisons and normal data at 0.5 poison ratio

C. Poison Ratio Larger Than 0.5

Finally, in this section, we discuss when the poison ratio is larger than 0.5. As in Sec. IV-B, the list-decodable setting is adopted, and the final output function is chosen as the one with the smaller validation MSE. Moreover, since over half of the data are poisons, f^*_w in (2) tends to fit the poisons instead of the normal data. We thus use the validation set to also determine the appropriate λ to set on line 6 in Alg. 1. Table V shows the configuration for each dataset and attack. We do not include Flip because it supports at most 0.5 poison ratio. The same list-decodable setting and search for appropriate λ are applied to iTRIM and Sever. However, $\lambda = 0.01$ for all of Huber's experiments since it does not support filtering out poisons.

Does our method still yield better partitions at poison ratios larger than 0.5? We show the precision and recall of our method and iTRIM in Table IV. In several cases other

TABLE IV: Precision / Recall (%) at poison ratios larger than 0.5

	Stability						DERMS					
	Opt		Add		Noise		Opt		Add		Noise	
ratio	Ours	iTRIM	Ours	iTRIM	Ours	iTRIM	Ours	iTRIM	Ours	iTRIM	Ours	iTRIM
0.6	71.2/**96.0**	**74.2**/73.6	**100**/**100**	**100**/99.2	96.5/**42.1**	**99.2**/20.3	92.2/**96.8**	**96.4**/94.5	**100**/**100**	**100**/94.7	66.4/6.0	**86.0**/**23.9**
0.7	74.5/**99.5**	**82.3**/73.5	**100**/**100**	**100**/99.2	98.1/**38.8**	**99.5**/19.6	95.8/**95.9**	**98.1**/94.6	**100**/**100**	**100**/95.2	75.3/6.0	**90.0**/**23.2**
0.8	82.2/**99.9**	**89.3**/74.4	**100**/**100**	**100**/99.2	99.0/**36.3**	**99.7**/19.1	95.7/**95.4**	**99.5**/94.2	**100**/**100**	**100**/94.7	85.9/6.2	**94.5**/**22.9**
0.9	91.5/**99.4**	**95.2**/71.4	**100**/**100**	**100**/99.2	99.6/**33.7**	**99.9**/18.5	97.0/**95.3**	**99.9**/94.0	**100**/**100**	**100**/94.2	93.2/5.8	**97.2**/**22.3**
	House						CCPP					
	Opt		Add		Noise		Opt		Add		Noise	
ratio	Ours	iTRIM	Ours	iTRIM	Ours	iTRIM	Ours	iTRIM	Ours	iTRIM	Ours	iTRIM
0.6	98.7/**99.2**	**100**/**99.2**	99.6/**100**	**100**/98.0	**93.0**/**40.6**	92.8/21.3	79.3/**99.4**	**92.3**/90.5	**100**/**100**	**100**/99.2	98.9/**42.8**	**99.5**/20.4
0.7	98.9/**99.3**	**100**/99.2	**100**/**100**	**100**/97.8	95.2/**37.9**	**95.6**/19.6	83.9/**99.5**	**95.6**/91.0	**100**/**100**	**100**/99.2	99.4/**39.7**	**99.7**/19.6
0.8	99.6/**99.3**	**100**/99.2	**100**/**100**	**100**/97.7	97.2/**35.0**	**97.6**/20.3	88.9/**99.3**	**97.4**/90.8	**100**/**100**	**100**/99.2	99.7/**36.6**	**99.8**/19.0
0.9	99.9/**99.2**	**100**/**99.2**	**100**/**99.9**	**100**/95.8	**98.8**/**32.7**	98.8/18.3	94.5/**98.9**	**99.0**/90.2	**100**/**100**	**100**/99.2	99.9/**34.1**	**99.9**/18.5

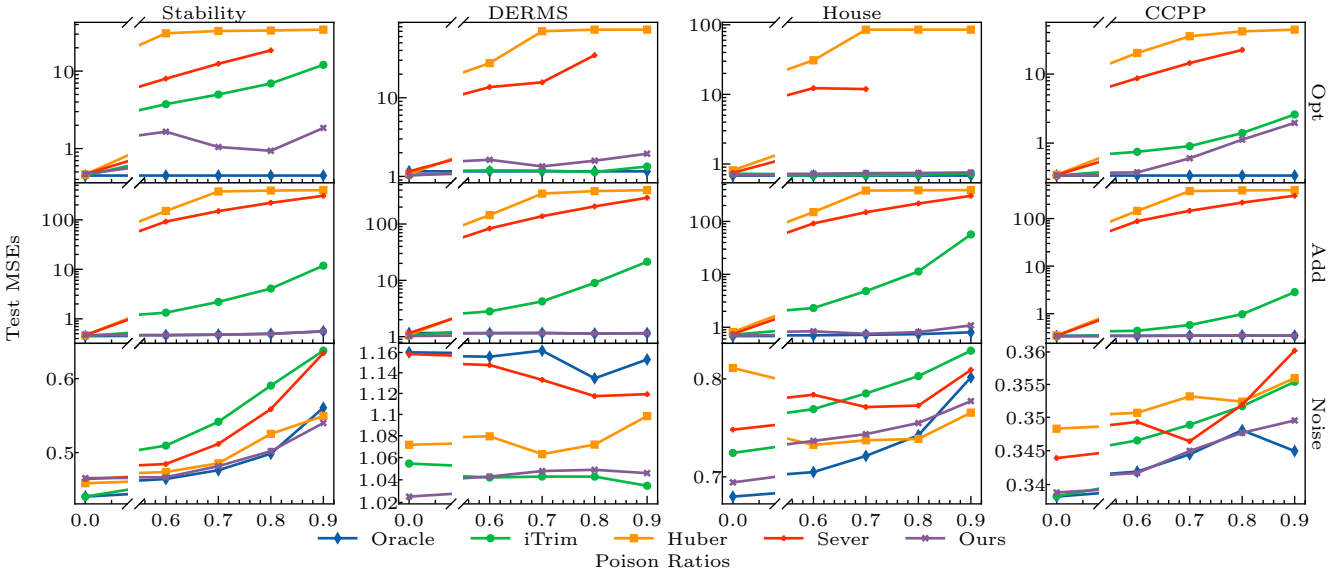

Fig. 3: **Test MSEs at poison ratios larger than 0.5.** According to Table IV, nearly 100% precision and recall on additive attack lead to the lowest test MSE. High recall benefits datasets without model misspecification (Stability and CCPP), while high precision benefits datasets with model misspecification (DERMS and House).

TABLE V: λ configurations at poison ratios larger than 0.5

	Stability			DERMS			House			CCPP		
	Ours	iTRIM	Sever	Ours	iTRIM	Sever	Ours	iTRIM	Sever	Ours	iTRIM	Sever
Opt	10^{-3}	10^{-2}	10^{-3}	10^{-3}	10^{-2}	10^{-3}	10^{-2}	10^{-2}	10^{-2}	10^{-2}	10^{-2}	10^{-1}
Add	10^{-2}	10^{-3}	10^{-2}	10^{-2}	10^{-2}	10^{-3}	10^{-2}	10^{-3}	10^{-2}	10^{-2}	10^{-3}	10^{-1}
Noise	10^{-1}	10^{-2}	10^{-1}	10^{-1}	10^{-2}	10^{-1}	10^{-2}	10^{-2}	10^{-1}	10^{-3}	10^{-2}	10^{-2}

than additive attack, where we have nearly perfect precision and recall, iTRIM yields higher precision but lower recall than our method. iTRIM's behavior of mistakenly excluding data in learning f was also observed in Table III, where iTRIM has generally higher recall than precision. Now that f learns the distribution of the poisons instead of the normal data, the poisons not captured by f lead to lower recalls. On the other hand, our method is able to include more poisons in learning f but at the same time mistakenly includes more normal data in learning f, which leads to lower precisions.

How do precision and recall affect resultant models in the presence and absence of model misspecification? We show the test MSEs in Fig. 3. It appears that when model misspecification exists, the MSEs benefit from iTRIM's method. Specifically, iTRIM has lower MSE on DERMS and House under optimization-based injection. However, our method achieves lower MSEs on Stability and CCPP. Nearly perfect precision and recall under additive attack also give us the lowest MSE across all datasets. As for noise corruption, Huber achieves the lowest MSE on House, iTRIM on DERMs, and our method on the datasets where there is no model misspecification. Furthermore, since optimization-based injection creates poisons in addition to the normal data, $\mathcal{D}$ becomes $10\times$ larger at 0.9 poison ratio. As a result, Sever runs out of memory on House at poison ratio 0.8 and all datasets at poison ratio 0.9.

V. Conclusion

In this research, we presented a bilevel optimization-based framework to counteract poisoning attacks targeting data-driven smart grid applications. Notably, our approach achieves high precision and recall in partitions for poison ratios below 0.5, culminating in models with the lowest test MSE, especially when no model misspecification exists. With an incorporated smoothness inductive bias, our method excels, registering the lowest test MSE at a 0.5 poison ratio. For elevated poison ratios, our method prioritizes recall, still benefiting the subsequent model in scenarios without misspecification. We further explored the impact of model inaccuracies due to autocorrelation across varied poison ratios. Looking forward, adapting the bilevel optimization for autoregressive models stands as a promising avenue to eliminate model discrepancies.

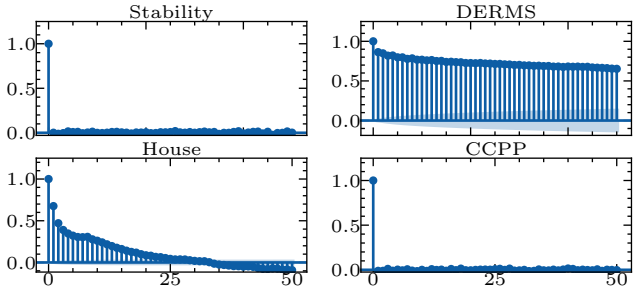

Fig. 4: **Autocorrelation function of the residuals of each dataset.**

APPENDIX A
AUTOCORRELATION IN THE DATASETS

For each dataset, we plot the autocorrelation function of the training residuals after fitting a kernel ridge regression model up until lag 50 in Fig. 4. The figure shows that Stability and CCPP are free of autocorrelation while House and DERMS are autocorrelated. This indicates the existence of model misspecification, where our kernel ridge regression does not capture the interaction between data points of different time stamps. In fact, any non-autoregressive model fails to capture autocorrelation.

APPENDIX B
DERIVATION OF $\frac{\partial H(W)}{\partial w_i}$

Since $H(w) = \frac{1}{\mathrm{Tr}(I-S(w))}(Y^\top(I-S(w))Y - 2\Lambda^\top(I-S(w))Y + \Lambda^\top(I-S(w))\Lambda)$, we take the derivative with respect to w_i for each term, and denote $s'(w_i) := s(w_i)(1-s(w_i))$.

$$\begin{aligned}
\tfrac{\partial}{\partial w_i}\tfrac{1}{\mathrm{Tr}(I-S(w))} &= \tfrac{s'(w_i)}{(\mathrm{Tr}(I-S(w)))^2} \\
\tfrac{\partial}{\partial w_i} Y^\top(I-S(w))Y &= -y_i^2 s'(w_i) \\
\tfrac{\partial}{\partial w_i} - 2\Lambda^\top(I-S(w))Y &= -2\tfrac{\partial \Lambda^\top}{\partial w_i}(I-S(w))Y \\
&\quad + 2\Lambda^\top(e_i s'(w_i) e_i^\top)Y \\
\tfrac{\partial}{\partial w_i}\Lambda^\top(I-S(w))\Lambda &= \tfrac{\partial \Lambda^\top}{\partial w_i}(I-S(w))\Lambda \\
&\quad - \Lambda^\top e_i s'(w_i) e_i^\top \Lambda \\
&\quad + \Lambda^\top(I-S(w))\tfrac{\partial \Lambda}{\partial w_i}.
\end{aligned} \tag{6}$$

To derive $\frac{\partial \Lambda}{\partial w_i}$, let $\Delta := (S(w)K + \lambda I)$.

$$\begin{aligned}
\tfrac{\partial}{\partial w_i}\Lambda &= \tfrac{\partial}{\partial w_i} K(S(w)K+\lambda I)^{-1} S(w)Y \\
&= K(\tfrac{\partial \Delta^{-1}}{\partial w_i} S(w)Y + \Delta^{-1}\tfrac{\partial S(w)}{\partial w_i}Y) \\
&= K(-\Delta^{-1}(e_i s'(w_i) e_i^\top K)\Delta^{-1} S(w)Y \\
&\quad + \Delta^{-1} e_i s'(w_i) e_i^\top Y) \\
&= -K\Delta^{-1} e_i s'(w_i) e_i^\top \Lambda + K\Delta^{-1} e_i s'(w_i) e_i^\top Y \\
&= K(S(w)K+\lambda I)^{-1} e_i s'(w_i)(e_i^\top(Y-\Lambda)).
\end{aligned} \tag{7}$$

Putting it all together, we have 4.

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